

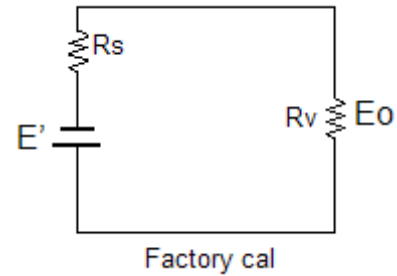
## DMMCheck Plus Voltage Reference

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Dec 2013

### Factory calibration.

$R_s := 25$  Source resistance  
 $R_v := 10^7$  DMM calibration resistance  
 $E_o := 5$  Cal value

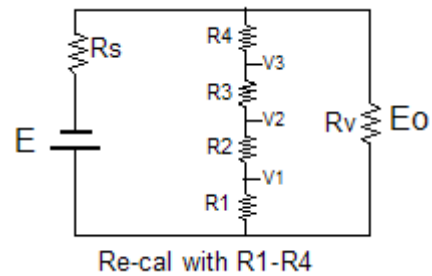
$E'$  is adjusted to read  $E_o = +5.0000$  V



### Re - calibration with divider, with load $R_v$

$E$  is re-adjusted to read  $E_o = +5.0000$  V

$R_1 := 100.04$        $R_2 := 1000.78$   
 $R_3 := 10002$        $R_4 := 100096$   
 $R := R_1 + R_2 + R_3 + R_4$



$$E_o = E \cdot \frac{\frac{R_v \cdot R}{R_v + R}}{\frac{R_v \cdot R}{R_v + R} + R_s}$$

$$E_o = R \cdot R_v \cdot \frac{E}{(R_v \cdot R + R_s \cdot R_v + R_s \cdot R)} \quad \text{Eq. 1}$$

Solve for  $E$ :

$$E := \frac{E_o}{R \cdot R_v} \cdot (R_v \cdot R + R_s \cdot R_v + R_s \cdot R) \quad \text{Eq. 2}$$

$E = 5.001137$       New  $E$  value to read  $E_o = +5.0000$  V

The thevenin resistance of source  $E$  is  $\sim R_s$ , since  $R$  and  $R_v \gg R_s$

### $E_{o1}$ with a different load: $R_{v1}$ , the voltmeter resistance

$R_{v1} := 10^6$

$$R_{Th4} := \frac{R \cdot R_s}{R + R_s} \quad R_{Th4} = 24.994$$

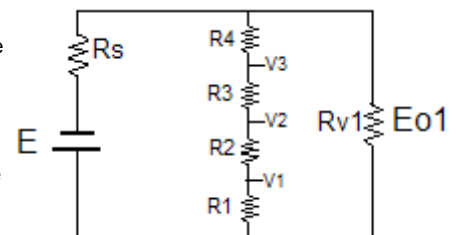
Eq. 3  
Thevenin resistance

$$V_{Th4} := E \cdot \frac{R}{R + R_s} \quad V_{Th4} = 5.000012$$

Eq. 4  
Open circuit voltage

$$E_{o1} := V_{Th4} \cdot \frac{R_{v1}}{R_{v1} + R_{Th4}} \quad E_{o1} = 4.999888$$

Eq. 5  
Voltage at  $E_{o1}$



### Voltage at V3, with RV1 connected at V3:

$$R_{Th3} := \frac{(R1 + R2 + R3) \cdot (R4 + R_s)}{R + R_s}$$

Eq. 7

Thevenin resistance

$$R_{Th3} = 9994.491$$

$$V_{Th3} := E \cdot \frac{(R1 + R2 + R3)}{R + R_s}$$

Eq. 8

Open circuit voltage

$$V_{Th3} = 0.499234$$

$$V3 := V_{Th3} \cdot \frac{R_{v1}}{R_{v1} + R_{Th3}}$$

Eq. 9

Voltage at V

$$V3 = 0.494294$$

### Voltage at V2, with RV1 connected at V2:

$$R_{Th2} := \frac{(R1 + R2) \cdot (R3 + R4 + R_s)}{R + R_s}$$

Eq. 10

Thevenin resistance

$$R_{Th2} = 1089.925$$

$$V_{Th2} := E \cdot \frac{(R1 + R2)}{R + R_s}$$

Eq. 11

Open circuit voltage

$$V_{Th2} = 0.049498$$

$$V2 := V_{Th2} \cdot \frac{R_{v1}}{R_{v1} + R_{Th2}}$$

Eq. 12

Voltage at V2

$$V2 = 0.049444$$

### Voltage at V1, with RV1 connected at V1:

$$R_{Th1} := \frac{(R1) \cdot (R2 + R3 + R4 + R_s)}{R + R_s}$$

Eq. 13

Thevenin resistance

$$R_{Th1} = 99.95$$

$$V_{Th1} := E \cdot \frac{(R1)}{R + R_s}$$

Eq. 14

Open circuit voltage

$$V_{Th1} = 0.004498$$

$$V1 := V_{Th1} \cdot \frac{R_{v1}}{R_{v1} + R_{Th1}}$$

Eq. 15

Voltage at V1

$$V1 = 0.004498$$

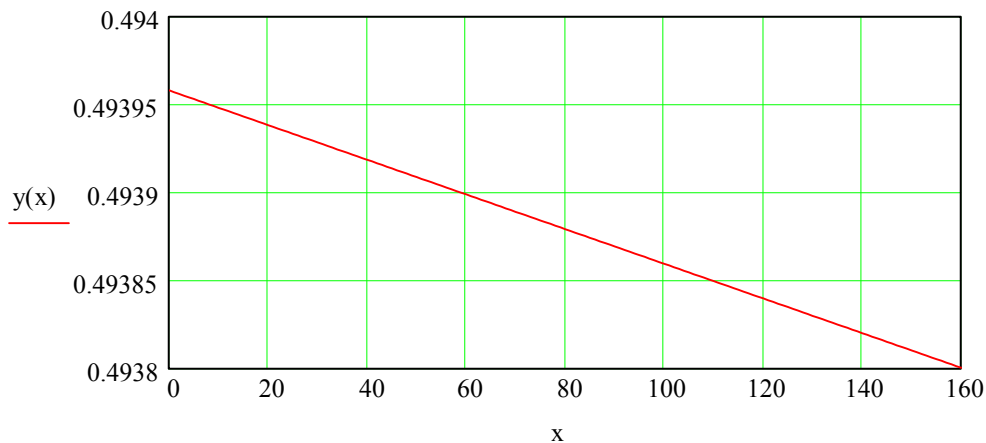
### Effect of Input Capacitance at AC 100 Hz on V3 voltage

From R<sub>dg</sub> vs pF.xls

$$y(x) := -9.848127 \cdot 10^{-7} \cdot x + 0.4939582$$

$$y = -9.848127E-07x + 4.939582E-01$$

$$x := 0, 1 \dots 160$$



$$y(60) = 0.4939$$

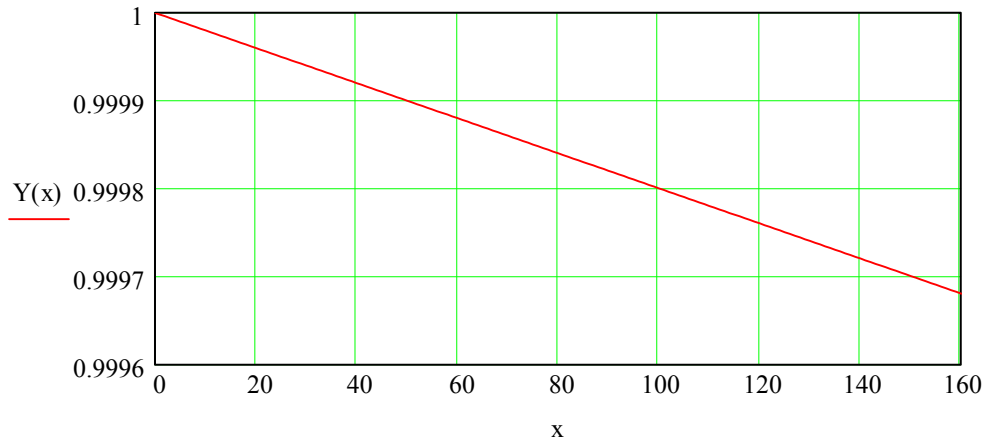
$$y(x) := -9.848127 \cdot 10^{-7} \cdot x + 0.4939582$$

$$Y(x) := \frac{-9.848127 \cdot 10^{-7}}{y(0)} \cdot x + \frac{0.4939582}{y(0)}$$

$$\frac{-9.848127 \cdot 10^{-7}}{y(0)} = -1.993717 \times 10^{-6}$$

$$Y(x) := -1.993717 \times 10^{-6} \cdot x + 1$$

$$\frac{0.4939582}{y(0)} = 1$$



Changed the sign of the slope

YY (x) is the mult factor to use to correct for the input capacitance

$$YY(x) := \frac{9.848127 \cdot 10^{-7}}{y(0)} \cdot x + \frac{0.4939582}{y(0)}$$

$$\frac{0.4939582}{y(0)} = 1$$

$$YY(x) := 1.994 \cdot 10^{-6} \cdot x + 1$$

