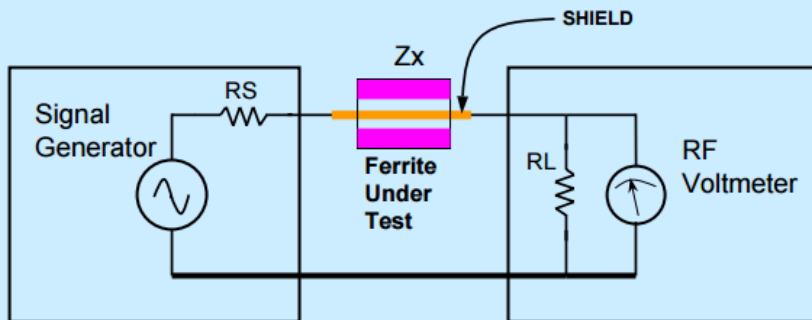


IMPEDANCE MEASUREMENTS

FREQUENCY RESPONSE MODE

- Does NOT allow measuring separately the Resistive and Inductive components
- Ease of sweeping the frequency
- Reference level = 0 dB = short in place of ferrite



RS and RL are generally 50 ohms

To calculate Zx from attenuation readings in + dB's:
(assumes that Zx is resistive)

$$Z_x = (R_L + R_S) \cdot \left(10^{\frac{\text{dB}}{20}} - 1\right)$$

Signal gen voltage: E

RF Voltmeter voltage: e1 at calibration, e2 with the ferrite inserted

$$e_1 = E \cdot \frac{R_L}{R_L + R_S}$$

Calculate the voltage divider

$$K_1 = \frac{e_1}{E} = \frac{R_L}{R_L + R_S}$$

K1 is the reference voltage ratio at calibration (called the 0 dB ref. level)

$$K_2 = \frac{R_L}{R_L + R_S + Z_x}$$

K2 is the voltage ratio with the ferrite inserted (will read some dB lower)

The linear attenuation caused by the ferrite is:

$$K = \frac{K_2}{K_1}$$

Using the equations for K1 and K2 above:

$$K = \frac{\frac{RL}{RL+RS+Zx}}{\frac{RL}{RL+RS}}$$

Note that K is ≤ 1

$$K = \frac{RL + RS}{RL + RS + Zx}$$

Simplify

$$Zx = \frac{RL + RS}{K} - RS - RL$$

Solving for Zx:

$$Zx = \frac{RL + RS - K \cdot (RL + RS)}{K}$$

Rearrange

$$Zx = \frac{(RL + RS) \cdot (1 - K)}{K}$$

Rearrange

$$K = 10^{\left(\frac{-dB}{20}\right)}$$

Computing K from the positive dB measured

$$Zx = \frac{(RL + RS) \cdot (1 - K)}{K}$$

Eq. repeated

$$Zx = (RL + RS) \cdot \left(\frac{1}{K} - 1\right)$$

Rearrange

$$Zx = \left(10^{\frac{dB}{20}} - 1\right) \cdot (RL + RS)$$

After substituting K from the dB, above

$$Zx = \frac{(RL + RS) \cdot (1 - K)}{K}$$

Eq. repeated

Note that: K = S21, the S parameter describing the transmission ratio.

$$Zx = \frac{(RL + RS) \cdot (1 - S21)}{S21}$$

Substitute S21 for K

With RL=RS=50 ohms, we get:

$$Zx = 100 \cdot \frac{(1 - S21)}{S21}$$

This is the equation that the VNA computes to display Zx in the series mode
 Note that the VNA measures S21 as a complex quantity:
 It has a magnitude and an angle or Real and Imaginary parts.

Example

$\text{dB} := 1, 1.1.. 50$

$\text{RL} := 50$

$\text{RS} := 50$

$$Z_x(\text{dB}) := \left(10^{\frac{\text{dB}}{20}} - 1 \right) \cdot (\text{RL} + \text{RS})$$

